

WAVE MECHANICS, FYSA13

Friday, June 5, 2020

Allowed material: The enclosed formulas and a calculator.

Total number of points: 20. Points required to pass: 10

The following values can be used in the problems below:

The speed of sound in air is 343 m/s and the density of air is 1.20 kg/m^3 . The speed of sound in water is 1484 m/s and the density of water is 997 kg/m^3 . The speed of light is $3.00 \times 10^8 \text{ m/s}$. The gravitational acceleration is 9.82 m/s^2 and $1 \text{ m/s} = 3.6 \text{ km/h}$.

V1

A 4.00 kg block hangs from a spring, extending it 16.0 cm from its unstretched position.

- What is the spring constant? (2p)
- The block is removed, and a 0.500 kg body is hung from the same spring. If the spring is then stretched and released, what is its period of oscillation? (2p)

V2

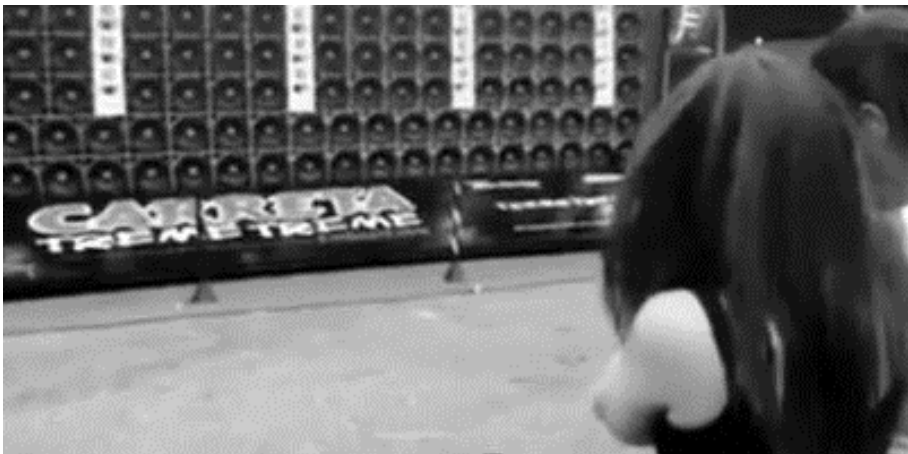
A string that is stretched between fixed supports separated by 75.0 cm has resonant frequencies (normal modes) of 420 and 315 Hz, with no intermediate resonant frequencies.

- What is the lowest resonant frequency? (2p)
- What will be the lowest resonant frequency if we double the tension in the string without changing anything else? (2p)

V3

Vincent has found a youtube video with the Brazilian loudspeaker truck Carreta Treme Treme in which a girl's hair is moved by the soundwaves (see photo below). To see if this can be true he makes a simple back-of-the-envelope calculation under the assumption of a sinusoidal sound wave with frequency 30 Hz and intensity level 130 dB.

- What will then be the displacement amplitude? (2 p)
- What will be the maximum pressure variations that the sound wave produces? (2 p)



V4

Light from a HeNe laser with a wavelength of 632.8 nm is sent to two narrow slits so that an interference pattern is formed on a screen located 3.00 meters from the slit. The maximum light intensity on the screen is 2.00 mW/mm^2 . The angles to the bright bands in the interference pattern on the screen are so small that one can make the approximation $\sin(\theta) = \tan(\theta) = \theta$ where θ is the angle between the normal to the plane of the slits and a line from the slits to a point on the screen.

- What is the distance between the slits if the angle to the middle of the first dark band on the screen is 0.2 degrees? (2 p)
- What is the smallest angle θ for which one will have an intensity of 0.70 mW/mm^2 (2 p)

V5

A low-pressure sodium lamp produces a light spectrum from the two sodium emission lines with 589.00 and 589.56 nanometres wavelength. It is studied with a 10 mm wide grating in a spectrometer like the one in the figure below.

- If the second-order diffraction line is found at $\theta = 64.56$ degrees for the 589.00 nm light, at what angle should one find the light from second-order diffraction of light with 589.56 nm wavelength ? (2 p)
- What chromatic resolving power is needed to see both emission lines at second order? What chromatic resolving power do we expect the grating to provide? (2 p)

